## Decision 2 Linear Programming Questions

5 (a) Display the following linear programming problem in a Simplex tableau.

$$
\begin{array}{lr}
\text { Maximise } & P=3 x+2 y+4 z \\
\text { subject to } & x+4 y+2 z \leqslant 8 \\
& x \geqslant 7 y+3 z \leqslant 21 \\
& x \geqslant 0, y \geqslant 0, z \geqslant 0 \tag{3marks}
\end{array}
$$

(b) Use the Simplex method to perform one iteration of your tableau for part (a), choosing a value in the $z$-column as pivot.
(c) (i) Perform one further iteration.
(ii) State whether or not this is the optimal solution, and give a reason for your answer.

5 A linear programming problem involving variables $x$ and $y$ is to be solved. The objective function to be maximised is $P=4 x+9 y$. The initial Simplex tableau is given below.

| $\boldsymbol{P}$ | $\boldsymbol{x}$ | $\boldsymbol{y}$ | $\boldsymbol{r}$ | $\boldsymbol{s}$ | $\boldsymbol{t}$ | value |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | -4 | -9 | 0 | 0 | 0 | 0 |
| 0 | 3 | 7 | 1 | 0 | 0 | 33 |
| 0 | 1 | 2 | 0 | 1 | 0 | 10 |
| 0 | 2 | 7 | 0 | 0 | 1 | 26 |

(a) Write down the three inequalities in $x$ and $y$ represented by this tableau.
(2 marks)
(b) The Simplex method is to be used to solve this linear programming problem by initially choosing a value in the $x$-column as the pivot.
(i) Explain why the initial pivot has value 1 .
(ii) Perform two iterations using the Simplex method.
(iii) Comment on how you know that the optimum solution has been achieved and state your final values of $P, x$ and $y$.

3 (a) Display the following linear programming problem in a Simplex tableau.

$$
\begin{array}{ll}
\text { Maximise } & P=5 x+8 y+7 z \\
\text { subject to } & 3 x+2 y+z \leqslant 12 \\
& 2 x+4 y+5 z \leqslant 16 \\
& x \geqslant 0, y \geqslant 0, z \geqslant 0
\end{array}
$$

(3 marks)
(b) The Simplex method is to be used by initially choosing a value in the $y$-column as a pivot.
(i) Explain why the initial pivot is 4.
(ii) Perform two iterations of your tableau from part (a) using the Simplex method.
(iii) State the values of $P, x, y$ and $z$ after your second iteration.
(iv) State, giving a reason, whether the maximum value of $P$ has been achieved.
(1 mark)

4 A linear programming problem involving variables $x$ and $y$ is to be solved. The objective function to be maximised is $P=3 x+5 y$. The initial Simplex tableau is given below.

| $\boldsymbol{P}$ | $\boldsymbol{x}$ | $\boldsymbol{y}$ | $\boldsymbol{s}$ | $\boldsymbol{t}$ | $\boldsymbol{u}$ | value |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | -3 | -5 | 0 | 0 | 0 | 0 |
| 0 | 1 | 2 | 1 | 0 | 0 | 36 |
| 0 | 1 | 1 | 0 | 1 | 0 | 20 |
| 0 | 4 | 1 | 0 | 0 | 1 | 39 |

(a) In addition to $x \geqslant 0, y \geqslant 0$, write down three inequalities involving $x$ and $y$ for this problem.
(b) (i) By choosing the first pivot from the $\boldsymbol{y}$-column, perform one iteration of the Simplex method.
(ii) Explain how you know that the optimal value has not been reached.
(1 mark)
(c) (i) Perform one further iteration.
(ii) Interpret the final tableau and state the values of the slack variables.

